Optimization of Logical Queries

Integrated Exercise 8.3 p3

Translate the following SQL query to the relational algebra, remove redundant joins and use the algebraic laws to produce a better query plan.

```
SELECT F.budget, E.eid
FROM Emp E, Dept D, Finance F
WHERE E.did = D.did AND D.did = F.did
  AND E.hobby = 'yodeling'
  AND D.floor NOT IN
  ( SELECT D2.floor FROM Dept D2, Finance F2
    WHERE NOT D2.dname = 'CID'
      OR  (F2.did = D2.did AND F2.expenses >= ALL
             (SELECT MAX(F3.expenses)
              FROM Finance F3
              WHERE F3.budget = F.budget)
          )
  )
```

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Step 1. Normalize to Exists and Not Exists

```
SELECT F.budget, E.eid
FROM Emp E, Dept D, Finance F
WHERE E.did = D.did AND D.did = F.did AND E.hobby = 'yodeling'
  AND NOT EXISTS
  ( SELECT D2.floor FROM Dept D2, Finance F2
    WHERE D.floor = D2.floor AND
      ( NOT D2.dname = 'CID'
        OR  (F2.did = D2.did AND NOT EXISTS
                (SELECT MAX(F3.expenses)
                 FROM Finance F3
                 WHERE F3.budget = F.budget
                 HAVING MAX(F3.EXPENSES) > F2.EXPENSES)
             )
      )
  )
```

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Step 2. Normalize to the conjunctive normal form

```
SELECT F.budget, E.eid
FROM Emp E, Dept D, Finance F
WHERE E.did = D.did AND D.did = F.did AND E.hobby = 'yodeling'
  AND NOT EXISTS
  ( SELECT D2.floor FROM Dept D2, Finance F2
    WHERE (D.floor = D2.floor AND NOT D2.dname = 'CID')
       OR (D.floor = D2.floor AND F2.did = D2.did
           AND NOT EXISTS
                (SELECT MAX(F3.expenses)
                 FROM Finance F3
                 WHERE F3.budget = F.budget
                 HAVING MAX(F3.EXPENSES) > F2.EXPENSES)
           )
  )
```

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Step 3. Normalize to UNION

```
SELECT F.budget, E.eid
FROM Emp E, Dept D, Finance F
WHERE E.did = D.did AND D.did = F.did AND E.hobby = 'yodeling'
  AND NOT EXISTS
  ((SELECT D2.floor FROM Dept D2, Finance F2
    WHERE D.floor = D2.floor AND NOT D2.dname = 'CID')
   UNION
    (SELECT D2.floor FROM Dept D2, Finance F2
     WHERE D.floor = D2.floor AND F2.did = D2.did
           AND NOT EXISTS
                 (SELECT MAX(F3.expenses)
                  FROM Finance F3
                  WHERE F3.budget = F.budget
                  HAVING MAX(F3.EXPENSES) > F2.EXPENSES)
    )
  )
```

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Step 4. Translation of the innermost subquery

```
SELECT MAX(F3.expenses)
FROM Finance F3
WHERE F3.budget = F.budget
HAVING MAX(F3.EXPENSES) > F2.EXPENSES)
```

$$e_1 := \boldsymbol{\pi}_{\texttt{MAX(F3.expenses),F.*,F2.*}}\, \boldsymbol{\sigma}_{\texttt{MAX(F3.expenses)>F2.expenses}}\, \boldsymbol{\gamma}_{\texttt{MAX(F3.expenses),F.*,F2.*}}$$
$$\boldsymbol{\sigma}_{\texttt{F3.budget=F.budget}}\, (\boldsymbol{\rho}_{\texttt{F}}(\texttt{Finance}) \times \boldsymbol{\rho}_{\texttt{F2}}(\texttt{Finance}) \times \boldsymbol{\rho}_{\texttt{F3}}(\texttt{Finance}))$$

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Step 5. Translation

```
(SELECT D2.floor FROM Dept D2, Finance F2
 WHERE D.floor = D2.floor AND F2.did = D2.did
       AND NOT EXISTS
            (SELECT MAX(F3.expenses)
             FROM Finance F3
             WHERE F3.budget = F.budget
             HAVING MAX(F3.EXPENSES) > F2.EXPENSES)
)
```

Translating the From clause yields: (note that F is a context relation!)

$$e_2 := \boldsymbol{\rho}_{\mathtt{D2}}(\mathtt{Dept}) \times \boldsymbol{\rho}_{\mathtt{F2}}(\mathtt{Finance}) \times \boldsymbol{\rho}_{\mathtt{D}}(\mathtt{Dept}) \times \boldsymbol{\rho}_{\mathtt{F}}(\mathtt{Finance})$$

Since this is a NOT EXISTS subquery, we decorrelate by means of an antijoin:

$$f_2 := (e_2 \,\overline{\bowtie}\, \pi_{\mathtt{F2.*,F.*}}(e_1))$$

Adding the WHERE and SELECT clauses (with the necessary parameters) gives:

$$e_3 := \boldsymbol{\pi}_{\mathtt{D2.floor,D.*,F.*}} \boldsymbol{\sigma}_{\mathtt{D.floor=D2.floor} \wedge \mathtt{F2.did=D2.did}}(f_2)$$

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Step 6. Translation

```
((SELECT D2.floor FROM Dept D2, Finance F2
  WHERE D.floor = D2.floor AND NOT D2.dname = 'CID')
```

$$e_4 := \boldsymbol{\pi}_{\texttt{D2.floor,D.*}} \boldsymbol{\sigma}_{\texttt{D.floor=D2.floor} \wedge \texttt{D2.name} \neq \texttt{'CID'}} (\boldsymbol{\rho}_{\texttt{D2}}(\texttt{Dept}) \times \boldsymbol{\rho}_{\texttt{F2}}(\texttt{Finance}) \times \boldsymbol{\rho}_{\texttt{D}}(\texttt{Dept}))$$

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Step 7. Translation of the union

```
((SELECT D2.floor FROM Dept D2, Finance F2
  WHERE D.floor = D2.floor AND NOT D2.dname = 'CID')
 UNION
  (SELECT D2.floor FROM Dept D2, Finance F2
   WHERE D.floor = D2.floor AND F2.did = D2.did
         AND NOT EXISTS
               (SELECT MAX(F3.expenses)
                FROM Finance F3
                WHERE F3.budget = F.budget
                HAVING MAX(F3.EXPENSES) > F2.EXPENSES)
  )
)
```

Notice that the schemas of e_3 and e_4 are not equivalent because they have other context relations. Therefore, to be able to take the union, we have to add the context relation F of e_3 to e_4.

$$e_5 := \pi_{\texttt{D2.floor,D.*,F.*}}(e_3) \cup \pi_{\texttt{D2.floor,D.*,F.*}}(e_4 \times \boldsymbol{\rho}_{\texttt{F}}(\texttt{Finance}))$$

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Step 8. Translation of the outermost query

Translation of the From clause yields:

$$e_6 := \boldsymbol{\rho}_{\mathtt{E}}(\mathtt{Emp}) \times \boldsymbol{\rho}_{\mathtt{D}}(\mathtt{Dept}) \times \boldsymbol{\rho}_{\mathtt{F}}(\mathtt{Finance})$$

Since this is a NOT EXISTS subquery, we decorrelate by means of an antijoin:

$$f_7 := e_6 \,\overline{\bowtie}\, \boldsymbol{\pi}_{\mathtt{D.*,F.*}}(e_5)$$

And translate the remaining WHERE and SELECT clauses:

$$e_7 := \boldsymbol{\pi}_{\mathtt{F.budget,E.eid}}(\boldsymbol{\sigma}_{\mathtt{E.did=D.did} \wedge \mathtt{D.did=F.did} \wedge \mathtt{E.hobby='yodeling'}}(f_7))$$

Whole expression:

$$\boldsymbol{\pi}_{\texttt{F.budget,E.eid}}($$
$$\boldsymbol{\sigma}_{\texttt{E.did=D.did}\wedge\texttt{D.did=F.did}\wedge\texttt{E.hobby='yodeling}}(\boldsymbol{\rho}_{\texttt{E}}(\texttt{Emp}) \times \boldsymbol{\rho}_{\texttt{D}}(\texttt{Dept}) \times \boldsymbol{\rho}_{\texttt{F}}(\texttt{Finance})))$$
$$\overline{\bowtie} \ (\boldsymbol{\pi}_{\texttt{D.*,F.*}} \boldsymbol{\sigma}_{\texttt{D.floor=D2.floor}\wedge\texttt{D2.name}\neq\texttt{'CID'}}(\boldsymbol{\rho}_{\texttt{D2}}(\texttt{Dept}) \times \boldsymbol{\rho}_{\texttt{F2}}(\texttt{Finance})$$
$$\times \boldsymbol{\rho}_{\texttt{D}}(\texttt{Dept}) \times \boldsymbol{\rho}_{\texttt{F}}(\texttt{Finance}))$$
$$\cup \ \boldsymbol{\pi}_{\texttt{D.*F.*}} \ ((\boldsymbol{\sigma}_{\texttt{D.floor=D2.floor}\wedge\texttt{F2.did=D2.did}}(\boldsymbol{\rho}_{\texttt{D2}}(\texttt{Dept}) \times \boldsymbol{\rho}_{\texttt{F2}}(\texttt{Finance})$$
$$\times \boldsymbol{\rho}_{\texttt{D}}(\texttt{Dept}) \times \boldsymbol{\rho}_{\texttt{F}}(\texttt{Finance})))$$
$$\overline{\bowtie} \ (\pi_{\texttt{F2.*,F.*}} \boldsymbol{\sigma}_{\texttt{MAX(F3.expenses)>F2.expenses}} \boldsymbol{\gamma}_{\texttt{MAX(F3.expenses),F.*,F2.*}}$$
$$\boldsymbol{\sigma}_{\texttt{F3.budget=F.budget}} \ (\boldsymbol{\rho}_{\texttt{F}}(\texttt{Finance}) \times \boldsymbol{\rho}_{\texttt{F2}}(\texttt{Finance}) \times \boldsymbol{\rho}_{\texttt{F3}}(\texttt{Finance}))))$$

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Step 9. Removal of redundant joins

No atom can be removed from the following maximal subexpressions (why?)

- $\boldsymbol{\sigma}_{\texttt{E.did=D.did}\wedge\texttt{D.did=F.did}\wedge\texttt{E.hobby='yodeling}}(\boldsymbol{\rho}_{\texttt{E}}(\texttt{Emp}) \times \boldsymbol{\rho}_{\texttt{D}}(\texttt{Dept}) \times \boldsymbol{\rho}_{\texttt{F}}(\texttt{Finance}))$
- $(\boldsymbol{\sigma}_{\texttt{D.floor=D2.floor}\wedge\texttt{F2.did=D2.did}}(\boldsymbol{\rho}_{\texttt{D2}}(\texttt{Dept}) \times \boldsymbol{\rho}_{\texttt{F2}}(\texttt{Finance}) \times \boldsymbol{\rho}_{\texttt{D}}(\texttt{Dept}) \times \boldsymbol{\rho}_{\texttt{F}}(\texttt{Finance})))$
- $\boldsymbol{\sigma}_{\texttt{F3.budget=F.budget}}(\boldsymbol{\rho}_{\texttt{F}}(\texttt{Finance}) \times \boldsymbol{\rho}_{\texttt{F2}}(\texttt{Finance}) \times \boldsymbol{\rho}_{\texttt{F3}}(\texttt{Finance})))))$

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Step 9. Removal of redundant joins

Subexpression

$$\pi_{\mathtt{D.*,F.*}}\, \sigma_{\mathtt{D.floor=D2.floor} \wedge \mathtt{D2.name} \neq \mathtt{'CID'}} (\rho_{\mathtt{D2}}(\mathtt{Dept}) \times \rho_{\mathtt{F2}}(\mathtt{Finance}) \times \rho_{\mathtt{D}}(\mathtt{Dept}) \times \rho_{\mathtt{F}}(\mathtt{Finance}))$$

Is not a select-project-join expression, because of the inequality. Therefore, no redundant join can be removed.

Therefore, in this example, no redundant join can be removed.

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Step 10. Application of the algebraic laws

$$\pi_{\texttt{F.budget,E.eid}}\Big(\pi_{\texttt{F.*,E.eid}}\Big(\pi_{\texttt{E.eid,e.did}}\sigma_{\texttt{E.hobby}=\texttt{'yodeling'}}\rho_{\texttt{E}}(\texttt{Emp}) \underset{\texttt{E.did}=\texttt{D.did}}{\bowtie} \pi_{\texttt{D.did}}\rho_{\texttt{D}}(\texttt{Dept}) \underset{\texttt{D.did}=\texttt{F.did}}{\bowtie} \rho_{\texttt{F}}(\texttt{Finance})\Big)\Big)$$
$$\overline{\bowtie}\ \Big(\pi_{\texttt{F.*}}\ \Big(\pi_{\texttt{D2.floor}}\sigma_{\texttt{D2.name}\neq\texttt{'CID'}}\rho_{\texttt{D2}}(\texttt{Dept}) \underset{\texttt{D.floor}=\texttt{D2.floor}}{\bowtie} \pi_{\texttt{D.floor}}\rho_{\texttt{D}}(\texttt{Dept}) \times \pi\rho_{\texttt{F2}}(\texttt{Finance}) \times \rho_{\texttt{F}}(\texttt{Finance})\Big)$$
$$\cup\ \pi_{\texttt{F.*}}\ \Big(\big(\pi_{\texttt{F.*,F2.*}}\big(\pi_{\texttt{D.floor}}\rho_{\texttt{D2}}(\texttt{Dept}) \underset{\texttt{D.floor}=\texttt{D2.floor}}{\bowtie} \pi_{\texttt{D2.floor,D2.did}}\rho_{\texttt{D}}(\texttt{Dept}) \underset{\texttt{F2.did}=\texttt{D2.did}}{\bowtie} \rho_{\texttt{F2}}(\texttt{Finance}) \times \rho_{\texttt{F}}(\texttt{Finance})\big)$$
$$\overline{\bowtie}\ \big(\pi_{\texttt{F2.*,F.*}}\sigma_{\texttt{MAX(F3.expenses)}>\texttt{F2.expenses}}\gamma_{\texttt{MAX(F3.expenses),F.*,F2.*}}$$
$$\big(\rho_{\texttt{F}}(\texttt{Finance}) \underset{\texttt{F3.budget}=\texttt{F.budget}}{\bowtie} \pi_{\texttt{F3.budget,F3.expenses}}\rho_{\texttt{F3}}(\texttt{Finance}) \times \rho_{\texttt{F2}}(\texttt{Finance})\big)\big)\big)\big)$$