Introduction to GeoVisualization {and Visual Analytics}

Special focus: spatio-temporal and movement data

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{Geo} Information Visualization, basic principles

Interactive Maps and Multiple Coordinated Views



Maps: not only for orientation!

People live in geographical space. Most of people's decisions and actions depend on

- where the things are;
- how are their locations related.

Maps allow people to perceive the space beyond the directly observable extent.

A map serves as a model of reality and helps to detect patterns existing in the reality





Example: Dr. John Snow's discovery



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Interactive maps

Interactive maps can change in response to user's actions

Many interactive maps are available on the Web, e.g. street maps, tourist maps, election maps, ...

Interaction techniques are used to

- compensate for the display deficiencies, e.g. limited size (zoom and pan, showing additional information related to mouse position, ...)
- increase the display expressiveness
- enable more sophisticated analyses



Typical interactive operations

Select information layers, e.g. on a tourist map: accommodation, museums, restaurants, nightlife

Select time moments or intervals in displays of time-related information, e.g. election year

Change the spatial scale, e.g. states or counties

Change the theme, e.g. president elections or governor elections, absolute values or differences in comparison to the previous time

Choose the visualization method, e.g. area painting or proportional symbols



Examples of analytical interactions





Removing Outliers (1)



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Removing Outliers (2)



After the removal of two outliers, the differences are better seen





Object Comparison



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Pattern Investigation (1)







Pattern Investigation (2)

By moving the slider, we see more patterns and gain more understanding of value distribution









Focusing and Visual Comparison on Other Map



Piechart Map

Applicable to several attributes that together give some meaningful whole

Contraction of the second seco

However, the map often looks like this:

"Pie" size is proportional to the total (sum of the attribute values)

Representation method: Pies
Census data
total employed in agriculture 1991
total employed in industry 1991
total employed in services 1991



The division into slices shows proportion of each attribute in the total

Here the population is very small in comparison to the large cities. Therefore, the pies are too small to be seen







Piechart Map: Focusing







Focusing and Data Investigation



In districts with much population people work in industry (magenta) and services (cyan).

Northwest: more industry

Centre-west: more services

At this stage, the agricultural part (green) becomes visible

In districts with little population considerable proportion of people works in agriculture, but services still prevail





Why to Use Multiple Views?





Parallel coordinates: object characteristics profiles; relationships between attributes (look at line slopes)

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Display Linking by Highlighting









Display Linking by Selection

Selection (durable highlighting) does not disappear after the mouse is moved away. One or more objects may be selected e.g. by mouse-clicking on them.







Using Display Linking (1)



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Using Display Linking (2)



Using Display Linking (3)

Let us look at the districts with the highest population growth:

Click on the rightmost bars in the histogram

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Dynamic Query

Dynamic query allows us to set constraints on attribute values







Dynamic Query in Action (1)











Dynamic Query in Action (2)

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A second query condition









Propagation of Object Classes







Propagation of Object Classes: Use Example



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years.

3.5%). For % employed in services we see the opposite relationship

Table View and Table Lens (1)

Pop. % pop. % pop. % pop. % pop. Pop. % pop. % pop. densitv densitv no. no with. with. with high with high 1981 1991 primary primary school school primary primary identifiers school school school school education education 2 education education education education 1981 1991 1991 1991 1981 1981 8.51 Lisboa 9636.423 7912.43 37.26 39.49 25.45 7.675 11.11 🔺 37.32 26.22 39.97 8,756 Porto 7858.089 7260.49 8.83 9.84 6895.481 7454.641 9.68 38.66 25.189.941Amadora 40.41 10.80 3257.592 3301.527 7.33 32.8013.83 Oeiras 37.89 18.69 10.444 28.16 39.09 10.089 9.85 2796.012 2723.485 40.64 10.01 Barreiro 7.78 Matosinhos 2190.979 2434.703 42.45 11.0140.12 29.08 9.857 2110.581 2169.072 40.58 10.26 25.99 8.813 Almada 38.49 10.66 Sao Joao da Madeira 2027.62 2275.216 41.1210.2139.62 28.59 9.658 7.68 27.50 7.56 1513.025 1631.933 44.68 11.37 35.82 10.919 Espinho Cascais 1457.75 1579.276 39.37 8.92 34.97 21.13 9.718 12.95 27.121419.716 1654.349 40.84 10.29 39.32 9.950 10.09 Loures 43.66 11.61 39.18 29.86 10.352 7.07 Vila Nova de Gaia 1324.968 1455.128 39.93 10.493 6.93 Gondomar 981.172 1074.426 43.2**0** 12.31 29.72 44.45 11.71 30.47 Maia 975.854 1112.915 39.08 10.4067.0737.64 26.617.71 46.27 14.50 9.123 Moita 966.594 1181.663 38.33 10.15 24.60 10.375 Seixal 952.844 1249.3 41.18 11.15 880.038 1016.194 Valondo 42.8**0** 11.90 39.94 30.70 11.492 6.40 9.10 26.73 11.22 👻 874.161 1038.394 38.51 40.18 7.952 Entroncamento Þ Descending 🗖 🇹 TableLens Sort by: Pop. density 1981 condensed Ŧ Attribute..

Click for sorting

Table cell shading shows the relative position of the values between the minimum and maximum values of the respective attributes





Table View and Table Lens (2)



The same information can be represented in a "condensed" form. We do not see the details about particular objects but get an overall impression about value variation and relationships between attributes.

High proportions of people having high school education often cooccur with high population density

Surprisingly, the districts with the lowest proportions of people having high school education in 1991 had much higher proportion of such people in 1981





Class Propagation to Table View (1)



example, that the general educational level tends to be higher in districts with high proportion of people employed in services



group by classes Sort by: % pop. with high V Descending V TableLens V condensed



Attribute.

Class Propagation to Table View (2)

Wara do Casisó % employed in services 1991 Yura do Casisó 20.12 35.00 50.00] 85.57 Automatic classification • Statistical quality • Classification statistics • Cumulative curve	Pop. density 1991	% pop. no primary school education 1981	% pop. no primary school education 1991	% pop. with primary school education 1981	% pop. with primary school education 1991	% pop. with high school education 1981	% pop. with high school education 1991
It may also be useful to switch the grouping off							
Broadcast classification Add to table Manipulate							

group by classes

We see that the red rows occur mostly at the top of the table and blue ones at the bottom. Note that the rows are sorted according to % people with high school education in 1991.

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Attribute.

Sort by: % pop. with high 🗸 Descending 👻 🗹 TableLens 🗹 condensed

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Summary

This lecture was supposed to

- introduce the concept of analytical interactive maps
- stress the importance of exploring various aspects of data using multiple views
- demonstrate some types of non-cartographic displays useful in analysis of geodata
- demonstrate various techniques of display linking
- show how to use this in data analysis



See also

Natalia and Gennady Andrienko • **Exploratory Analysis of Spatial and Temporal Data** A Systematic Approach Springer-Verlag, December 2005

section 4.8, pp.428-449







Data structure

So far:

Id, x, y, attribute(s)

Let's add one more special component: time

• Id, x, y, t, attribute(s)




Overview

Types of Analysis Tasks on Spatio-Temporal Data

Three primary task foci (target information)

- Focus on objects
- Focus on space
- Focus on time

Two types of task subject

- Characteristics
- Relations

Two levels of analysis

- *Elementary*: focus on one or more elements of a set
- Synoptic: focus on a set as a whole, disregard individual elements
- Task may be elementary w.r.t. one subject and synoptic w.r.t. another







Data Types and Transformations

Methods & Techniques for Different Spatio-Temporal Data









Data Types and Transformations

Methods & Techniques for Different Spatio-Temporal Data



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Spatial Time Series

Data structure



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High level analysis questions



Spatial Time Series (STS)

How are attribute values distributed over the territory at a given time moment?

How do the attribute values at a given place vary over time?

How does the overall spatial pattern of value distribution evolve over time?

How are different behaviour patterns distributed over the territory? Are there spatial clusters of similar behaviours?



Spatial Time Series



Methods & Techniques for Different Spatio-Temporal Data I

Visualization methods

- Animated maps
- "Layman techniques": (animated) charts embedded in maps (bar charts, pie charts, …)
- "<u>Small multiples</u>" map displays
- Time Graphs and their transformations



Spatial Time Series



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Time Map



8 × Data transformation For a time map, States /iolent Crime rate Compare to: one can use any Representation method: Alaska Max: 1245 Unclassified choropleth representation map 2922 Crime statistics method suitable Violent Crime rate Montana for static data. Nebraska n Utah 1245 Choropleth maps Total: 52 objects Territory: USA are good for Background 10 Min: exploring spatial 7.76 m Dynamic map update Time controls distribution Compare by click in 1960 2000 this map patterns. Manipulate lh 990 CommonGIS 1998-2003: USA Crime stati: Step 1 Q. Delay 0 \land \lor

Spatial Time Series: Basic Visualization Methods I

Time-dependent data may be represented on a <u>time map</u>, which is manipulated through time controls and, in particular, allows animation





When time map is useful



Spatial Time Series: Basic Visualization Methods I



How did the spatial distribution pattern develop over time?

At moment *t*, how were the values distributed over the whole space?

At what time moment were the values distributed over the space in the given manner?



Map Series



Spatial Time Series: Basic Visualization Methods I



To compare the spatial distributions of attribute values at two or more time moments, we need to see these distributions simultaneously. Best of all is to use multiple maps displayed in a common panel and manipulated through a common set of controls.

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Exploring the Distribution of Changes

Spatial Time Series: Data Transformations



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Map Series: Useful Transformations











Spatial Time Series: Data Transformations

Build map series with transformed data: relative difference to median value

Spatial distribution patterns of attribute values may become more vivid

Value and patterns evolution over time can be seen more easily





Spatial Time Series



Methods & Techniques for Different Spatio-Temporal Data I

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States

Value Flow Map

Spatial Time Series: Basic Visualization Methods II









Value Flow Map (2)











Value Flow Map (2)



Spatial Time Series: Basic Visualization Methods II









Temporal Behavior Exploration



Spatial Time Series: Data Transformations

As with time maps, various transformations can be applied to value flow maps



Here: comparison to each country's mean

- For every time moment, each state's values is replaced by its difference to the country's overall mean value at that moment
- Yellow color corresponds to positive differences, and blue negative



Value Flow Map Disadvantages

Spatial Time Series: Basic Visualization Methods II

The diagrams are perceived as separate entities \rightarrow the map must be

The diagrams are perceived as separate entities \rightarrow the map must be scanned and cannot be grasped as a single image

Absence of ordering complicates seeking for specific behaviour patterns

Diagram overlapping is a serious problem









- seeing the temporal behaviors in their spatial context
- seeing all behaviors at once
- detecting behaviors with particular features
- noticing what sorts of features exist in the data

Spatial Time Series



Methods & Techniques for Different Spatio-Temporal Data I

Visualization methods

- Animated maps
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- "Small multiples" map displays
- Time Graphs and their transformations





























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Spatial Time Series: Data Transformations



mtana

Burglary rate; year=1960

Burglary rate; year=1975

Burglary rate; year=1990

Alaska

Alaska

Alaska





Texas



















Spatial Time Series



Methods & Techniques for Different Spatio-Temporal Data I

Visualization methods

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Time Graph



Spatial Time Series: Basic Visualization Methods III

Putting all behaviors together makes their comparison more convenient

Numeric details on-demand by pointing on an object's line

Plus, to better understand general development trends :

- "mean behavior line" connecting means of each year
- "median behavior" connecting the year medians

Time graph 2: Crime statistics	Time graph 4: Crime statistics
Motor vehicle theft rate	Burglary rate
1840 1995 11 District of Columbia: 1840 0 0 1960 1963 1966 1969 1972 1975 1978 1981 1984 1987 1990 1993 1996 1999	2907 2000 1000 0 1960 1963 1966 1969 1972 1975 1978 1981 1984 1987 1990 1993 1996 1999
🔲 Show only selected objects 🗹 Value flow 🗹 Value classes 🗹 Grid	🔲 Show only selected objects 🗹 Value flow 🗹 Value classes 🗹 Grid
Statistics: 🗹 Average 🗌 Median Quantiles: 2 🔽 🗌 Save	Statistics: 🗹 Average 🗌 Median Quantiles: 🛛 💌 Save
Time extent Display Comparison Smoothing Segmentation Classification Selection	



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Time Graph: Multiple View Comparisons

Spatial Time Series: Basic Visualization Methods III



Juxtaposed time graphs are suitable for <u>comparing trends</u> and temporal variations of <u>two or more attributes</u>

This example shows that attributes "Motor vehicle theft rate" and "Burglary rate" have quite different trends of general development





Time Graph: Multiple View Comparisons

Spatial Time Series: Basic Visualization Methods III



Additionally employ <u>smoothing</u> (value averaging over intervals)Mitigates small fluctuationsExposes trends more clearly





Time Graph: Level of Detail



Spatial Time Series: Basic Visualization Methods III





Mean and median lines only give very coarse picture of the general value variation properties

For a finer analysis, may also look at the <u>quartiles</u> or even smaller <u>percentiles</u>.





Linked Views: Map + Time Graph



Spatial Time Series: Basic Visualization Methods IV

At place L_1 , how did the values behave over the entire time period?





Compare the temporal behavior at places L_1 and L_2









Time Graph++: Time Histogram



Spatial Time Series: Basic Visualization Methods V







Time Graph++: Time Histogram



Spatial Time Series: Basic Visualization Methods V

Time histograms facilitate comparison of 2 (or more) attributes

Compare temporal trends despite differences in value ranges



Here: attributes "Burglary rate" and "Motor vehicle theft rate"






Time Histogram of Changes

Spatial Time Series: Basic Visualization Methods VI

Transform attribute values into relative differences Apply aggregation by value intervals to the transformed values Encode values using <u>partitioned color scale</u>







Time Histogram of Changes



Spatial Time Series: Basic Visualization Methods VI







See also

Natalia and Gennady Andrienko
 Exploratory Analysis of Spatial and Temporal Data
 A Systematic Approach
 Springer-Verlag, December 2005

Chapter 4







An Introduction to Visual Analytics

Special focus: movement data

Gennady Andrienko Natalia Andrienko http://geoanalytics.net





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Definition of Visual Analytics



Visual Analytics:

the science of analytical reasoning facilitated by interactive visual interfaces

People use visual analytics tools and techniques to

- Synthesize information and derive insight from massive, dynamic, ambiguous, and often conflicting data
- Detect the expected and discover the unexpected
- Provide timely, defensible, and understandable assessments
- Communicate assessment effectively for action

The book (IEEE Computer Society 2005) is available at http://nvac.pnl.gov/

Analytical reasoning =

data \rightarrow information \rightarrow knowledge \rightarrow explanation (interpreted data) (for myself) (for others)

Illuminating the Path

Research and Development Agenda Visual Analytics

Edited by James J. Thomas and Kristin Cook







Visual Analytics:

divide the labor between the computers and humans to use the best of each

Computers

- can store and process great amounts of information
- are very fast in searching information
- are very fast in processing data
- can extend their capacities by linking with other computers
- can efficiently render high quality graphics, both static and dynamic

Humans

- are flexible and inventive, can deal with new situations and problems
- can solve problems that are hard to formalise
- can reasonably act in cases of incomplete and/or inconsistent information
- can simply see things that are hard to compute
- can employ their previous knowledge and experience



Visual Analytics:

the importance of visualisation

Visualise = make perceptible to human's mind

- "An estimated 50 percent of the brain's neurons are associated with vision. Visualisation <...> aims to put that neurological machinery to work."
 - B. McCormick, T. DeFanti, and M. Brown. Definition of Visualization. ACM SIGGRAPH Computer Graphics, 21(6), November 1987, p.3
- An abstractive grasp of structural features is the very basis of perception and the beginning of all cognition."
 - R. Arnheim. Visual Thinking.
 University of California Press, Berkeley 1969, renewed 1997, p. 161

(in other words: seeing already includes analyzing)

⇒ Visualisation is essential for enabling human analysts to use their inherent cognitive capabilities



Visual Analytics technology:

combining methods for visual and computational analysis

Goal: enable synergistic work of humans and computers





Visual Analytics: a summary

Defined as the science of analytical reasoning facilitated by interactive visual interfaces

Analytical reasoning \approx data \rightarrow information \rightarrow knowledge \rightarrow explanation (interpreted data) (for myself) (for others)

- The challenge of huge and complex data: distil relevant information and connections between them; gain insight from data!
- Visual Analytics (VA) combines interactive visualisations with computational processing
 - database processing, data mining algorithms, statistics, geographical analysis methods, ...
- VA focuses on the division of labour between humans and machines:
 - Computational power amplifies human perceptual and cognitive capabilities
 - Visual representations are the most effective means to convey information to human's mind and prompt human cognition and reasoning
- Hence, VA may be more broadly defined as the science of human-computer data analysis, knowledge building, and problem solving



Data Types and Structures



Everything begins with data

Analytical reasoning =

data \rightarrow information \rightarrow knowledge \rightarrow explanation

- **Data:** factual information (as measurements or statistics) used as a basis for reasoning, discussion, or calculation (Merriam-Webster dictionary)
- **Structured data:** collection of items (records) consisting of components of the same kinds; can be represented in a tabular form

Name	Birth date	School grade	Address	Distance to school, m	Getting to school
Peter	17/05/2005	3	12, Pine street	850	by bus
Julia	23/08/2004	4	9, Oak avenue	400	on foot
Paul	10/12/2005	2	56, Maple road	1500	by car
Mary	06/10/2003	5	71, Linden lane	900	on foot



Types of components in data

* Stevens, S.S. (1946). "On the Theory of Scales of Measurement". Science 103 (2684): 677–680.

Types of values:

- Numeric
- Textual
 - Predefined values (e.g., codes)
 - Free text
- Spatial
 - Coordinates
 - Place names
 - Addresses

Temporal

• Other (image, video, audio, ...)

Scales of measurement*:

- Nominal (¬ order, ¬ distances)
 - gender, nationality, ...
- Ordinal (✓ order, ¬ distances)
 - evaluations: bad, fair, good, excellent
- Interval (✓ order, ✓ distances, ¬ ratios, ¬ meaningful zero)
 - temperature, time, ...
- Ratio (✓ order, ✓ distances, ✓ ratios,
 ✓ meaningful zero)
 - quantities, distances, durations, ...

	Name	Birth date	School grade	Address	Distance to school, m	Getting to school	
	Peter	17/05/2005	3	12, Pine street	850	by bus	
	Julia	23/08/2004	4	9, Oak avenue	400	on foot	
	Paul	10/12/2005	2	56, Maple road	1500	by car	
Fraunhofer-Inst Analyse- und In	Mary	06/10/2003	5	71, Linden lane	900	on foot	Fraunhoter
, ,					EST 1894	_	

Semantic roles of data components

Reference: What is described?

- Object (physical or abstract)
- Place
- Time unit
- Object \times time unit
- Place × time unit
- Generally: anything specified as a single element or combination
- **Characteristic**, or **attribute**: What is known about it?

	Name	Birth date	School grade	Address	Distance to school, m	Getting to school	
	Peter	17/05/2005	3	12, Pine street	850	by bus	
	Julia	23/08/2004	4	9, Oak avenue	400	on foot]
	Paul	10/12/2005	2	56, Maple road	1500	by car	
Frau	Mary	06/10/2003	5	71, Linden lane	900	on foot	ofer
		•	•	EST 1894	•		

In our example:

the data describe children denoted by their names

Data may have two or more references

Refe	rence: tim	ne										
	Reference	e: plac	<u>e</u>				<u>Att</u>	<u>ributes</u>				
\downarrow (\							/				
year	id State	Population	Index offenses	Violent crime	Murder	Forcible rape	Robbery	Aggravated assault	Property crime	Burglary	Larceny-theft	Motor vehicle theft
1960	1 Alabama	3266740	39920	6097	406	281	898	4512	33823	11626	19344	2853
1960	2 Alaska	226167	3730	236	23	47	64	102	3494	751	2195	548
1960	4 Arizona	1302161	39243	2704	78	209	706	1711	36539	8926	23207	4406
1960	5 Arkansas	1786272	18472	1924	152	159	443	1170	16548	5399	10250	899
1960	6 California	15717204	546069	37558	616	2859	15287	18796	508511	143102	311956	53453
1960	8 Colorado	1753947	38103	2408	73	229	1362	744	35695	9996	21949	3750
1960	9 Connecticut	2535234	29321	928	41	103	236	548	28393	8452	16653	3288
1960	10 Delaware	446292	9642	375	33	41	157	144	9267	2661	5867	739
1960	11 District of Co	763956	20725	4230	81	111	1072	2966	16495	4587	9905	2003
1960	12 Florida	4951560	133919	11061	527	403	4005	6126	122858	39966	73603	9289
	•											
1972	54 West Virgini	1781000	25584	2299	109	146	562	1482	23285	7356	13976	1953
1972	55 Wisconsin	4520000	133382	4358	126	376	1661	2195	129024	28862	89642	10520
1972	56 Wyoming	345000	10461	511	14	48	117	332	9950	2057	7190	703
1973	1 Alabama	3539000	91389	12390	468	751	2809	8362	78999	31754	39206	8039
1973	2 Alaska	330000	16313	1269	33	147	221	868	15044	3852	9456	1736
1973	4 Arizona	2058000	137966	9877	167	637	3031	6042	128089	40301	76560	11228
1973	5 Arkansas	2037000	56149	5905	180	398	1456	3871	50244	18088	29204	2952
1973	6 California	20601000	1298872	116563	1862	8357	49531	56813	1182309	407824	643488	130997
1973	8 Colorado	2437000	133933	10088	193	944	3970	4981	123845	38963	70931	13951
1973	9 Connecticut	3076000	112717	6421	102	342	2589	3388	106296	31661	58742	15893
	1											
2000	44 Phode Island	10/9210	26444	2121	45	412	922	17/2	22222	6620	22029	4665
2000	45 South Carolia	4012012	200492	22202	100	1511	5002	24666	177100	20000	122038	15207
2000	45 South Dakot	75/10/12	17511	1259	233	205	121	24000	16252	20000	125054	10207
2000	40 South Dakota	5600000	270210	40222	/ /10	2196	9465	20172	227095	56244	15/111	27520
2000	47 Tennessee	20051020	1022210	112652	1220	7956	20257	74202	010659	100075	627522	27550
2000	40 TEXas	20031020	00050	5711	1230	962	1242	2562	94247	1/2/10	72/20	5/61
2000	50 Vormont	600027	10105	501	43	140	1242	3303	17/0/	2501	12194	0401
2000	51 Virginia	7070515	21/2/9	100/2	401	140	6205	423	19405	20424	1/6159	17012
2000	52 Washington	529/121	214340	217943	106	2727	5210	12042	279144	52/176	190650	25010
2000	54 West Virgini	18092//	300332 A7067	5722	150	2/3/	7/0	15045	273144 A12AA	9200	29120	2215
2000	55 Wisconsin	5362675	170107	10700	160	1165	/42	6020	150/07	25192	110605	1/626
2000	56 Wyoming	/02702	1/2124	1216	105	1105	4337	1074	1/1050	20100	12210	14030
2000	Johnvyonning	473/62	10265	1310	12	100	70	EST 1894	14505	2076	12310	375

Common classes of data structures

according to the types of the references

• **Object-referenced data**: attributes of objects

- **Events**: attributes include time of existence (moment or interval)
- **Spatial objects**: attributes include spatial location (point, area, or volume)
- **Spatial events**: attributes include existence time and location
- Time-referenced data, a.k.a. time series: attributes observed in different times (moments or intervals)
- Space-referenced data, a.k.a. spatial data: attributes observed in different places
- **Object time series**: attributes of objects observed in different times
 - Trajectories of moving objects: time series of spatial locations
- **Spatial time series**: attributes observed in different places and times





Multidimensional data

- Data including multiple attributes
- May have various types of references: objects, places, times, combinations ...
- Multiple attributes referring to times: multidimensional time series
- Multiple attributes referring to places: multidimensional spatial data
- Multiple attributes referring to places + times: multidimensional spatial time series



Classes of spatio-temporal data

Include space and time as references or characteristics

- Reference: objects; attributes: existence time + location + ...
 → spatial events
 - Earthquakes, mobile phone calls, public events, ...
- References: places + times; attributes: ...
 → spatial time series
 - Weather, population census data for different years, election results, ...
- References: objects + times; attributes: location + ...
 → trajectories
 - Trajectories of people, animals, vehicles, icebergs, hurricanes, ...



Running example dataset: DCTD trajectories of cars in Milan

GPS-tracks of 17,241 cars in Milan, Italy

Time period: from Sunday, the 1st of April, to Saturday, the 7th of April, 2007

Received from Octo Telematics <u>www.octotelematics.com</u> special thanks to Tina Martino

Data structure:

- Anonymized car identifier
- Date and time
- Geographic coordinates
- Speed

The trajectories from one day are drawn on a map with 5% opacity







Spatial events

🗖 ident	Longitude	Latitude	Start time	Duration (minutes)
1	9.149877	45.435764	04/04/2007 12:18:59	404
2	9.118851	45.405876	04/04/2007 04:30:18	305
3	9.153637	45.384422	04/04/2007 05:50:05	539
4	9.088079	45.526165	04/04/2007 06:38:20	241
5	9.088102	45.52614	04/04/2007 12:07:45	331
6	9.224027	45.529514	04/04/2007 06:47:07	186
7	9.230214	45.545048	04/04/2007 11:03:16	318
8	9.27865	45.46803	04/04/2007 06:24:51	385
9	9.088983	45.533787	04/04/2007 06:00:37	248
10	9.08896	45.53379	04/04/2007 11:27:47	304
11	9.225346	45.528656	04/04/2007 12:29:03	388
12	9.135795	45.486305	04/04/2007 05:14:31	607
13	9.080329	45.539093	04/04/2007 07:19:02	456
14	9.208277	45.46646	04/04/2007 13:45:37	282
15	9.188722	45.473045	04/04/2007 18:42:53	209
16	9.172471	45.38386	04/04/2007 04:34:31	476

References: objects Attributes: existence time + location + ...

Examples: earthquakes, mobile phone calls, public events, car stops, traffic jams, ...





Spatial events may be extended in time and/or space

e.g., traffic jams



	extent, m	Begin time	End time	Duration, minutes	
1	1909.82	04/04/2007 05:04:56	04/04/2007 08:08:19	183.4	
2	291.75	04/04/2007 05:22:46	04/04/2007 05:39:20	16.6	
3	734.22	04/04/2007 05:06:35	04/04/2007 05:41:35	35.0	
4	576.55	04/04/2007 05:08:45	04/04/2007 05:46:38	37.9	
5	491.55	04/04/2007 05:33:43	04/04/2007 06:03:21	29.6	
6	143.53	04/04/2007 05:35:34	04/04/2007 05:45:41	10.1	
7	459.94	04/04/2007 05:38:42	04/04/2007 06:07:08	28.4	
8	473.88	04/04/2007 15:11:05	04/04/2007 15:56:18	45.2	
9	358.59	04/04/2007 15:41:36	04/04/2007 16:16:29	34.9	
10	1256.72	04/04/2007 10:32:13	04/04/2007 12:45:12	133.0	
11	270.41	04/04/2007 12:14:09	04/04/2007 12:23:01	8.9	
12	371.49	04/04/2007 06:00:20	04/04/2007 06:06:14	5.9	Ŧ





Spatial time series

References: places + times; attributes: any

Example: number of cars that visited the regions of Milan in different hours of a day

	hour=00:	hour=01:	hour=02:	hour=03:	hour=04:	hour=05:	hour=06:	hour=07:	hour=08:	hour=09:	hour=10:	hour=11:	hour=12:	hour=13:	hour=14:	hour=15:	hour=16:	hour=17:	hour=18:	hour=19:	hour=20:	hour=21:	hour=22:	hour=23:
🗖 identifie	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N	N
	visitors																							
	by hours																							
Centre	68	45	46	116	272	630	935	928	852	878	890	791	812	885	883	926	1007	956	725	479	407	413	292	177
North	24	25	20	65	203	394	478	420	362	384	423	420	431	395	419	490	521	477	330	212	157	145	106	61
South	11	7	22	47	102	191	250	265	207	218	222	200	216	236	240	261	248	260	178	97	85	74	57	38
West	18	14	17	42	98	219	314	263	230	211	240	215	259	231	249	258	304	295	162	107	80	88	49	33
East	12	15	28	68	144	262	314	279	257	229	227	261	275	264	311	300	330	281	202	126	102	99	64	46
Northeast	29	27	28	78	233	437	538	512	464	492	462	446	504	445	497	515	540	523	359	222	203	169	130	62
Northwest	24	19	21	72	197	397	506	425	341	371	382	361	427	367	425	493	499	449	261	187	154	127	88	50
Southwest	18	14	19	37	111	208	327	304	247	236	265	245	240	276	264	338	335	301	198	108	82	72	50	35
Southeast	12	8	27	47	102	185	234	228	168	184	172	190	186	191	207	181	218	205	128	95	69	65	32	34



Data structure: (region, hour) \rightarrow number of cars



Spatial time series

viewed as spatially distributed local (location-associated) time series



Spatial time series

viewed as a temporal sequence of spatial situations

Numbers of cars in the regions in different hours are represented by proportional sizes of the circle symbols. A sequence of spatial situations may be visualised using an animated map (right) or multiple maps each showing one time moment or interval (below).





Trajectories

temporal sequences of spatial positions of discrete objects

	Carid	point N	longitude	latitude	time
1	104876	. 1	9 119127	45 558304	04/04/2007 06:45:15
2	104876	2	9142448	45 559753	04/04/2007 06:48:49
3	104876	3	9 156955	45 554962	04/04/2007 06:54:54
4	104876	4	9.156504	45.55017	04/04/2007 07:00:12
5	104876	5	9.156504	45.55017	04/04/2007 07:11:08
6	104876	6	9.156844	45.547703	04/04/2007 07:13:26
7	104876	7	9.156909	45,547688	04/04/2007 07:19:23
8	104876	8	9.162037	45,554867	04/04/2007 07:40:02
9	104876	9	9.167628	45.55907	04/04/2007 08:02:32
10	104876	10	9.172845	45.555725	04/04/2007 08:05:38
11	104876	11	9.172696	45.555492	04/04/2007 10:03:31
12	104876	12	9.166886	45.54498	04/04/2007 10:09:38
13	104876	13	9.163299	45.557983	04/04/2007 10:12:05
14	104876	14	9.162168	45.554855	04/04/2007 10:13:51
15	104876	15	9.162158	45.55487	04/04/2007 11:36:23
16	104876	16	9.162622	45.557976	04/04/2007 12:08:17
17	104876	17	9.16232	45.55496	04/04/2007 12:09:19
18	104876	18	9.162361	45.554943	04/04/2007 15:30:22
19	104876	19	9.122161	45.55825	04/04/2007 15:38:51
20	110800	1	9.266509	45.386322	04/04/2007 05:21:45
21	110800	2	9.261211	45.40307	04/04/2007 05:22:57
22	110800	3	9.247442	45.418125	04/04/2007 05:24:13
23	110800	4	9.254333	45.43362	04/04/2007 05:29:45
24	110800	5	9.257282	45.451492	04/04/2007 05:32:44
25	110800	6	9.252168	45.468708	04/04/2007 05:34:21
26	110800	7	9.251433	45.48671	04/04/2007 05:35:48
27	110800	8	9.258238	45.504066	04/04/2007 05:37:05
28	110800	9	9.260647	45.522255	04/04/2007 05:38:26
29	110800	10	9.278728	45.53516	04/04/2007 05:39:48
30	110800	11	9.274316	45.533176	04/04/2007 11:57:53
31	110800	12	9.261258	45.519493	04/04/2007 11:59:21
32	110800	13	9.256271	45.502003	04/04/2007 12:00:51
33	· · · · ·	_		_	12:02:11
34	– R <i>i</i>	eference	s' ohiect	s + timeg	<u>12:03:32</u>
35			5. 00jeot		12:04:53
36		tributoo	onatial la	nontion 1	12:06:14
37	al	indutes.	spallal IC	Jualion +	12:07:39
38	1		•		12:08:54
39	110800	20	9.270314	45.382904	04/04/2007 12:10:10
40	116291	1	9.234817	45.508648	04/04/2007 18:01:18
41	116291	2	9.257177	45.51305	04/04/2007 18:06:57
42	116291	3	9.255232	45.498352	104/04/2007 18:09:05 👻





Trajectories



Spatio-temporal view

Trajectories



Exercise: visual exploration of trajectories

Data: a small sample of daily trajectories

- Visualise the trajectories on a map and in a space-time cube.
- Find stops in the space-time cube.
- Select some trajectories on the map (by clicking) and examine their shapes on the map and in the space-time cube. Rotate the cube when needed for better seeing the trajectory shapes.



Interactive Techniques for Exploration of Spatio-Temporal Data

Focus: Interactive Filtering



Spatial filtering

by a rectangular "spatial window"





Spatial filtering

by areas from a map layer



Temporal filtering





Filtering by attributes





Start region			
identifiers	Overall frequency	Frequency after filtering	Ratio (%)
Vortheast	1722	355	20.62
Centre	1587	0	0.00
Vorthwest	1354	322	23.78
Southwest	808	170	21.04
East	737	182	24.69
Southeast	711	133	18.71
North	537	105	19.55
Vest	480	97	20.21
South	375	104	27.73
End region			

identifiers	Overall frequency	Frequency after filtering	Ratio (%)
Centre	1865	1468	78.71
Northeast	1520	0	0.00
Northwest	1347	0	0.00
Southeast	826	0	0.00
Southwest	754	0	0.00
East	580	0	0.00
North	546	0	0.00
Vest	479	0	0.00
Bouth	394	0	0.00

Dynam	nic Query fo	r Trajectori	es from 04/04/2007 (*	10 min break): genera	al data 🛛 🗶	
) yes	Start regio	on			19.1% : 1587 from 8311	
no	list 🖣	Centre"		Change		
) yes	End regio	n			77.6% : 6446 from 8311	
no	list 🖣	Centre"		Change		
			,		14.3% : 1190 from 8311	
Filt	er out miss	ing values	Clear all filters	🔽 Display	statistics 🔲 Dynamic update	
		Add attribu	ites	Remove attributes	~	



Sah Glacom

Start region

🗖 identifiers	Overall frequency	Frequency after filtering	Ratio (%)
Northeast	1722	0	0.00
Centre	1587	1190	74.98
Northwest	1354	0	0.00
Southwest	808	0	0.00
East	737	0	0.00
Southeast	711	0	0.00
North	537	0	0.00
West	480	0	0.00
South	375	0	0.00

End region

🗖 identifiers	Overall frequency		Frequency after filtering		Ratio (%)	
Centre		1865		0		0.00
Northeast		1520		229		15.07
Northwest		1347		305		22.64
Southeast		826		157		19.01
Southwest		754		134		17.77
East		580		117		20.17
North		546		70		12.82
West		479		88		18.37
Courth		204		0.0		22.04

Notes concerning interactive filtering

- Works not only for trajectories but for all types of data, including spatial events, places and place-related data, and flows between places
- Not only maps but all data displays react to filtering and show its results
- ⇒ Hence, filtering can be used to explore data by portions using multiple displays that show different aspects of the data
- There are also other types of interactive filters
- There are many other types of interactive exploratory techniques





Exercises on filtering

Data: trajectories divided into trips by 10 minutes break

Select trajectories passing near the Linate airport on the east of the city. How many such trajectories exist?



- Select trajectories visiting the regions Northwest, North, and Northeast. Select trajectories visiting these regions in the given order, then in the opposite order. Select trajectories that did not visit any of these regions.
- Find how many cars were under way in the time intervals 03:00-05:00, 05:00-07:00, 12:00-14:00, 18.00-20:00
- Select trajectories with the length of at least 25 km. How many of them visit the region Centre?


Data Transformations



Variety of data transformations

for a variety of purposes

For supporting abstraction

- Simplification: reduce excessive detail and high-resolution fluctuations
- Generalization: transform to larger units
 - E.g., time moments \rightarrow intervals; points \rightarrow areas; individual nominal values \rightarrow categories
- **Grouping** of similar and/or close items: elements \rightarrow subsets
- Aggregation: summarize values by larger units or by groups of items
- For managing large data volumes
 - Sampling; generalization; grouping; aggregation
- For obtaining task-relevant information
 - Computation of derived attributes
 - Feature extraction
 - E.g., trajectories \rightarrow movement events, time series \rightarrow trends, peaks, pits, ...



Some examples of data transformations



(Aggregate) moves, or flows





Link (short for 'spatial link')::= a spatial object representing directed relation, such as movement, between 2 locations.

A link is specified by a pair (origin place, destination place).

Links may have attributes such as number of moving objects, number of transitions, movement speed, ...

Links with attributes describing collective movements are called flows.

Flows may be represented on a map by half-arrow symbols with widths proportional to numeric attribute values.

Spatial time series of flows::= attribute values of the links in different time moments or intervals:

((origin, destination), time) \rightarrow

object count, transition count, speed, ...





equal flows in



unequal flows in two opposite directions

Transformations of spatio-temporal data structures



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VA support to data transformations

Example: generalization and spatio-temporal aggregation of trajectories



VA support to data transformations

Example: extraction of spatial events from trajectories



Exercises with transformed data (1)

Data: spatial time series of flows obtained by aggregating trajectories

- Visualise the total numbers of moves between places by line thicknesses (widths of flow symbols)
- Select (by filtering) the links where the total N of moves is not less than 200
- Visualise the dynamics of the average speeds by line thicknesses on an animated map display
- By animating the map, find cases when movement speeds between two places in two opposite directions substantially differ



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Visualize the speed dynamics on a time graph. Select the links marked on the images and describe the respective speed dynamics over the day.



Exercises with transformed data (2)

Data: spatial point events obtained by extracting trip ends from trajectories

- Observe the spatial distribution of the events on a map. Where do you see event concentrations?
- Observe the spatio-temporal distribution of the events in a space-time cube (STC). What patterns in the STC correspond to the point concentrations on the map?
- Using "spatial window" filter, select the point concentration near the Linate airport on the east. Describe the corresponding pattern in the STC. Are the events distributed evenly in time or there are temporal concentrations and temporal gaps?



Aggregate the events by the regions and hourly time intervals. Visualize the time series of event counts on a map by temporal diagrams ("value flow diagrams"). What regions have the largest numbers of events? In what regions there are peaks in the morning, in the afternoon, both?



Clustering



What is clustering?

- Loose definition: clustering is the process of organising objects into groups whose members are close or similar in some way.
- A cluster is a group of objects which are "similar" or "close" between them and are "dissimilar" or "distant" to the objects belonging to other clusters.



Example: clusters of spatially close points



Example: clusters of trajectories similar in the followed routes



Example: clusters of similar time series and clusters of links similar in their time series



Role of clustering in VA

Grouping of similar or close items plays an essential role in VA

- as a tool supporting <u>abstraction</u>: elements → subsets; the subsets may be considered as wholes
- as a tool to manage <u>large data volumes</u>
- as a tool to <u>study the behaviour</u> of attributes (i.e., distribution of attribute values) over the set of references, particularly,
 - multiple attributes
 - spatial and spatio-temporal positions of objects (events)
 - dynamic (time-variant) attributes, such as
 - time series of numeric values
 - trajectories of moving objects



Two major types of clustering

- Partition-based clustering: divide items into groups so that items within a group are similar (close) and items from different groups are less similar (more distant)
 - Examples: k-means, self-organizing map
 - Property of the result: each item belongs to some group
- Density-based clustering: find groups of highly similar (close) items and separate from them items that are less similar (more distant) to others
 - Examples: DBScan, OPTICS
 - Properties of the results: some items belong to groups, other items remain ungrouped and are treated as "noise"





Two major types of clustering: an example



Partition-based: convex clusters including all objects



Density-based: dense clusters of arbitrary shapes; many objects are treated as "noise" (gray)



Partition-based clustering

k-means: partitions data into k groups (k is a parameter specified by the user)



Problem: what value of k to choose?

In general: for any computational technique, what parameter settings to choose?

- Typically not known in advance
- Computation results (in particular, clusters) need to be properly visualised, to allow examination by the user
- The user needs to run the tool with different settings and see how the results change
- The user then selects the settings bringing the "best" results:
 - easy to interpret (e.g., understandable spatial patterns)
 - internal variance within the clusters is sufficiently low
 - fit to the purpose (e.g., the intended analysis scale may require coarser or finer division)
- Different visualizations are needed for different types and structures of data
 - Clustering results are often represented by colour-coding, which is applied to different visual objects, depending on the structure of the input data





Visualization of clustering results

A single display may be not enough

K-means clustering of spatial events according to the spatial and temporal positions (x, y, time)



Clustering may be applied to multiple and diverse attributes



Example: 12 k-means clusters of trajectories grouped according to the x- and y-positions of the start points, end points, and points in the middle of the paths, plus path lengths and spatial extents (i.e., lengths of the bounding rectangle diagonals).

Clusters by multiple attributes may be explored and interpreted using parallel coordinates plot



Clusters are selected one by one through filtering. It is also possible to select two clusters for comparison.



Clusters by time series of numeric attribute values can be explored using a time graph



Density-based clustering (DBC)

Goal: find dense groups of close or similar objects

- An object is treated as a core object of a cluster if there are at least N objects within the distance (radius) R around it. These objects are called neighbours.
- To make a cluster, (1) some core object with all its neighbours is taken; (2) for each core object already included in the cluster, all its neighbours are also added to the cluster (if not added yet).
- Some objects may remain out of any cluster (when they have not enough neighbours and do not belong to the neighbourhood of any core object). These objects are treated as "noise".
- For DBC, the user needs to specify the neighbourhood radius R and the minimum number of neighbours N. Therefore, the use of DBC requires an understandable definition of **distance** between objects, e.g., spatial distance or spatio-temporal distance. It may be hard to choose R for a more abstract "distance" between combinations of values of multiple diverse attributes.
- Results of DBC greatly depend on the parameter choice. Visualisation and interactive exploration help to find suitable values for R and N that lead to good results.



Exploring the impact of the DBC parameters

Example: DBC according to the spatial distances between points (trip ends)

R=500m, N=10



The clusters are too loose and too extended in space.

R=250m, N=10

R=300m, N=10



Some clusters are still too loose.



The clusters are more or less OK.

R=100m, N=10



The clusters are nicely compact but, possibly, too small and too few.

Spatio-temporal distance in DBC

Example: clustering of trip ends according to distances in space and time

For any two objects, there is a distance in space d_{space} and a distance in time d_{time} .

The user specifies two neighbourhood radii R_{space} and R_{time} , e.g., R_{space} = 300 m and R_{time} = 30 minutes. The clustering algorithm requires a single distance and a single radius; therefore, spatial and temporal distances need to be combined together, for example, as d = max(d_{space}/R_{space}, d_{time}/R_{time}) * R_{space}.



Spatio-temporal clusters of trip ends have been obtained with R_{space} = 300 m, R_{time} = 30 minutes, and N = 5. That is, two events are treated as neighbours if the distance in space between them is not more than 300m and the distance in time is not more than 30 minutes. A core object of a cluster must have at least 5 neighbours.

Some clusters last in time for almost the whole day, others have shorter life times. There are clusters sharing the same area in space but disjoint in time.



Distances between trajectories

- Trajectories are complex objects consisting of multiple spatio-temporal points, having origins and destinations, particular shapes, lengths, durations, and dynamically changing movement directions and speeds.
- It is hardly possible to define a distance measure that accounts for all these properties. Even if it could be defined, it would be hard to understand. Hence, it would be quite difficult to choose a meaningful value of R for clustering (as in the case of multiple diverse attributes).
- It is more feasible to create a library of simple distance measures (a.k.a. distance functions) addressing different properties. For example,
 - spatial distance between origins and/or between destinations,
 - average spatial distance between corresponding points along the routes,
 - average spatial distance between points reached at the same times, ...
- Different aspects of trajectories are studied using different distance functions.



DB clusters of trajectories (example 1)

Distance function: the average spatial distance between the origins and between the destinations; R=750m, N=5 Only 18 largest clusters are shown.



Summarised representation of clusters of trajectories

Minor flows are omitted for a clearer view.



DB clusters of trajectories (example 2)

Distance function: "route similarity", i.e., the average spatial distance between the corresponding points along the route; R=750m, N=5 Only 18 largest clusters are shown.



The same clusters represented in a summarised form



Two major types of clustering: a reminder

- Partition-based clustering: divide items into groups so that items within a group are similar (close) and items from different groups are less similar (more distant)
 - Examples: k-means, self-organizing map
 - Property of the result: each item belongs to some group
- Density-based clustering: find groups of highly similar (close) items and separate from them items that are less similar (more distant) to others
 - Examples: DBScan, OPTICS
 - Properties of the results: some items belong to groups, other items remain ungrouped and are treated as "noise"





Use of the two types of clustering

Partition-based:

- unites elements into subsets for
 - abstraction
 - decomposition of the analysis task and reduction of analytical workload
 - data aggregation
- integrates multiple attributes, allows comparison of items in terms of multiple attributes

Density-based:

- separates what is common, frequent from what is specific, infrequent
 - may be a tool for studying attribute behaviours (distributions)
 - concentrations of close/similar objects may have special meanings
 - e.g., spatio-temporal cluster of low speed events \Rightarrow traffic jam



Interactive visual support to clustering

Trying various parameter setting; studying parameter impact



Interactive visual support to clustering

Trying various parameter setting; studying parameter impact

- Interactive interface to a clustering tool
- Immediate visualization of clustering results
- Selection of clusters for close inspection and comparison
- Visual displays of the components used for the clustering allow the analyst to assess the internal variation in the clusters
 - In our example: numeric time series
- Visual displays of other data components supports interpretation of the clusters
 - In our example: map
- Positions of cluster centres can be projected onto a coloured plane
 - Shows distances (amounts of difference) between the clusters
 - Cognitively beneficial colour assignment: close clusters receive similar colours



Division of selected clusters with high internal variation



Applying different distance measures

Data: trajectories of cars in Milan

Step 1: clustering according to the spatial proximity of the end points

Question: what are the most frequent destinations of car trips?







Applying different distance measures (2)

Data: one (or more) selected cluster(s) from the previous step Step 2: clustering according to the similarity of the routes (shapes) Question: what routes are usually taken to get to the selected destination?





Purposes

- Controlled refinement of previously obtained clusters for
 - reducing internal variation
 - more detailed investigation of data subsets of interest
- Study of a set of complex objects with heterogeneous properties
 - application of diverse distance measures addressing different properties
 - a single distance measure would be hard to implement and results would be hard to interpret
 - incremental construction of multifaceted knowledge by progressively considering different properties


Exercises on applying clustering (k-means)

Data: spatial time series obtained by aggregating trajectories

- Visualise the time series of the average speeds of the traffic flows on a time graph. Apply k-means to the time series. Take k=7; observe on the map how the clustering separates the flows along the motorways from the flows in other parts of the city.
- Try k=8. Have the spatial patterns changed? Have the flows along the motorways been affected by the change of k?
- By selecting clusters one by one (through filtering), observe on the time graph which clusters have low internal variation (i.e., the lines are close to each other) and in which clusters the internal variation is higher. What can be said about the variation in the motorway-related clusters? What are the differences in the speed variation between these clusters?
- Try to refine the motorway-related clusters by progressive clustering: select only these clusters (let the number be m) and apply the k-means tool with setting k=m+2. Observe on the map and in the time graph how the clusters have been divided.
- On what motorways and in what directions are the average movement speeds the lowest?



Exercises on applying density-based clustering

Data: trajectories divided into trips by 10 minutes break

- Apply OPTICS clustering by trip destinations (i.e., end points of the trajectories) with R=250 m and N=10.
- Represent the resulting clusters in a summarized form. Try summarisation using all trajectory points and summarisation using only start and end points.
- What are the three most frequent trip destinations? Is there a cluster of trips ending in the centre? How many trajectories does it include?
- Progressive clustering: apply (in groups) clustering with the distance function "route similarity" to the four largest clusters obtained before (one cluster per group). Take R=750 m and N=5. Describe the most frequently taken routes to the respective destination areas.



Where to read more about visual analytics and about analysis of movement data

Springer, June 2013 ISBN 978-3-642-37582-8 397 p. 200 illus., 178 in colour

Gennady Andrienko · Natalia Andrienko Peter Bak · Daniel Keim · Stefan Wrobel

Visual Analytics of Movement

Ch.1. Introduction

- Ch.2. Conceptual framework
- Ch.3. Transformations of movement data
- Ch.4. Visual analytics infrastructure
- Ch.5. Visual analytics focusing on movers
- Ch.6. Visual analytics focusing on spatial events
- Ch.7. Visual analytics focusing on space
- Ch.8. Visual analytics focusing on time
- Ch.9. Discussion and outlook



🕗 Springer

Multi-perspective analysis of movement

Movement data can be viewed from multiple complementary perspectives.

Multi-perspective analysis allows deeper and more comprehensive understanding of the studied phenomenon, e.g., city traffic.

Trip destinations, routes...





Concluding summary

- Visual analytics tools and techniques support human analysts in performing data analysis: Data \rightarrow Information \rightarrow Knowledge \rightarrow Explanation
- VA tools and techniques enable analysts to exploit effectively their visionbased cognitive capabilities
 - Abstraction, grasping general, characteristic features, pattern detection and interpretation, ...
- VA tools and techniques divide the analytical labour between humans and computers
 - Use computer processing where human judgement is not needed
 - Use computers to prepare data to human analysis
 - Use computers to present data to analysts in the most suitable form



Multi-perspective Analysis of Movement Data with Visual Analytics

Gennady Andrienko Natalia Andrienko

http://geoanalytics.net





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Visual Analytics

Enabling synergetic work of humans and computers







Types of spatio-temporal data



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Transformations of spatio-temporal data structures



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Transformations enable multi-perspective analysis of movement data







Running example dataset: DCTO The reliable way trajectories of cars in Milan

GPS-tracks of 17,241 cars in Milan, Italy

Time period: from Sunday, the 1st of April, to Saturday, the 7th of April, 2007

Received from Octo Telematics www.octotelematics.com special thanks to T.Martino

Data structure:

- Anonymized car identifier
- Date and time
- Geographic coordinates
- Speed

The trajectories from one day are drawn on a map with 5% opacity







Perspective 1: Movement data in the form of trajectories



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Density-based clustering of trajectories: What distance measure to use?

- Trajectories are time series of spatial positions and other movement attributes
- Trajectories are complex objects with heterogeneous properties: positions in space and in time, shape, dynamics of speed, ...
- A single distance measure accounting for all properties would be hard to implement and results would be hard to interpret
- It is more feasible to create a library of simple distance measures (a.k.a. distance functions) addressing different properties. For example,
 - spatial distance between origins and/or between destinations,
 - average spatial distance between corresponding points along the routes,
 - average spatial distance between points reached at the same times, ...
 - Different aspects of trajectories are studied using different distance functions.



DB clusters of trajectories (example 1)

Distance function: the average spatial distance between the origins and between the destinations; R=750m, N=5 Only 18 largest clusters are shown.



Summarised representation of clusters of trajectories

Minor flows are omitted for a clearer view.



DB clusters of trajectories (example 2)

Distance function: "route similarity", i.e., the average spatial distance between the corresponding points along the route; R=750m, N=5 Only 18 largest clusters are shown.



The same clusters represented in a summarised form



Interactive progressive clustering

Applying different distance measures at different steps

Data: trajectories of cars in Milan

Step 1: clustering according to the spatial proximity of the end points Distance function: "common ends"

Question: what are the most frequent destinations of car trips?





Interactive progressive clustering

Applying different distance measures (2)

Data: one (or more) selected cluster(s) from the previous step Step 2: clustering according to the similarity of the routes (shapes) Distance function: "route similarity"

<u>Question</u>: what routes are usually taken to get to the selected destination?





Clustering of very large sets of trajectories

- Problem: clustering of complex objects (such as trajectories) involving nontrivial distance functions (such as "route similarity") can only be done in RAM, i.e. for a relatively small dataset
- Our approach:
 - 1. Take a subset (sample) of the objects suitable for processing in RAM.
 - 2. Discover clusters in the subset.
 - Load the remaining objects into RAM by portions. <u>Classify</u> each object = identify to which of the discovered clusters the object belongs. Store the result of the classification in the database.
 - 4. Take the objects that remained unclassified and apply steps 1 to 3 to them. Repeat the procedure until no meaningful new clusters can be discovered.
- Question: how to identify the cluster where an object belongs?



Classifier, the main idea

- From each cluster C_i select one or more representative objects (prototypes) and respective distance thresholds:
 - { (pt₁, d₁), ..., (pt_n, d_n) } such that $\forall o \in C_i \exists k, 1 \le k \le n$: distance (o, pt_k) < d_k
 - The set of all cluster prototypes with the respective distance thresholds defines the <u>classifier</u>
- A new object o' may be ascribed to the cluster if the same condition holds for it. \Rightarrow For each object from a large database:
 - measure the distances to all prototypes;
 - take the closest prototype among those with the distances below the thresholds and ascribe the object to the respective cluster;
 - if no such prototypes found, label the object as unclassified.
- To select prototypes:
 - Divide the cluster into "round" subclusters
 - Take the medoid of each subcluster as one of the prototypes
 - Take the maximum of the distances from the subcluster medoid to the subcluster members as the distance threshold for this prototype



Dividing a cluster into round sub-clusters: an illustration using points



This can be done by a variant of the K-medoids clustering algorithm where the desired maximum radius of a subcluster is a parameter.



Division of a cluster of trajectories into "round" subclusters

25.09.2009 11:05:24 - Cluster 7

naredo

Maximum subcluster radius х To select appropriate cluster prototypes, the density-based clusters will be divided into "round" subclusters Maximum radius of a subcluster? 1000.0 ΟK



prototype ID	Distance threshold	Original subcluster	N	Mean	Mean
			neighbours	distance to	distance to
			found in	the original	the found
		5120	the test	neigbours	neigbours
89133	438.2	4	0	240.5	0
96013	200.0	8	0	96.9	0
6548	526.5	29	0	161.1	0
43285	200.0	1	0	0.0	0
34239	414.3	19	0	186.7	0
32809	368.2	15	0	121.2	0
141138	485.0	10	0	271.3	0
109120	200.0	1	0	0.0	0



Dugnano



6548





141138

Opera



Dugnano



To obtain meaningful results, the analyst may needs to review and, possibly, edit the classifier



Example of interactive editing





What are the most frequent routes on Wednesday?

Result of clustering of single-day trajectories by route similarity



How frequent are these routes during the whole week?

Result of building a classifier and applying it to the whole set of trajectories



Further analysis of the trajectories

- The analysis is continued by loading a subset of the unclassified trajectories ("noise") to RAM, applying clustering to it, building a new classifier, and applying the classifier to the whole set of unclassified trajectories.
- Empirical experience:
 - With each new iteration step, the number and the sizes of discovered clusters substantially decrease in comparison to the previous step.
 - After 4-5 steps of the procedure, only very small clusters can be discovered.
 - The analyst's effort needed for editing of the classifier also decreases.
 - The editing effort is high for big clusters with high internal variation, which mostly appear in the first step; the following clusters are smaller and "cleaner".
- Unfortunately, no formal criterion for terminating the procedure.



Where to read more

G.Andrienko, N.Andrienko, S.Rinzivillo, M.Nanni, D.Pedreschi, F.Giannotti
Interactive Visual Clustering of Large Collections of Trajectories *IEEE Visual Analytics Science and Technology (VAST 2009)*Proceedings, IEEE Computer Society Press, 2009, pp.3-10



Analysis of movement attributes

Investigate speed variation along a selected route: single day





Analysis of movement attributes

Investigate speed variation along a selected route: whole week



Perspective 2: Movement data in the form of spatial events





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Example of analysis focusing on movement events

Data: trajectories of cars in Milan



- Task: find places of traffic congestions and determine their characteristics (times of the congestions, durations, numbers of cars involved, ...)
- Traffic congestion ~ dense spatio-temporal cluster of low speed movement events
 - Movement direction must be taken into account
- Places of interest: areas where at least one traffic congestion occurred ~ areas containing the clusters
- Characteristics of places: time series of event counts, vehicle counts, ...
- Data transformations:

Trajectories \rightarrow Events \rightarrow Places \rightarrow Spatial time series



Step 1: extract low speed events from the trajectories



Low speed := speed \leq 10 km/h





Vertical dimension \leftarrow time

Step 2: density-based clustering of events

by spatio-temporal positions and directions

Distance function:

$$d = \begin{cases} \infty, & \text{if } (d_s > D_s) \text{ or } \exists i \mid (d_i > D_i), \quad i = 0..n \\ \\ D_s * max \left(\frac{d_s}{D_s}, \frac{d_0}{D_0}, ..., \frac{d_n}{D_n}\right), & \text{if } (a) - \text{neighbourhood defined as a cube} \\ \\ D_s * \sqrt{\left(\frac{d_s}{D_s}\right)^2 + \sum_{i=0}^n \left(\frac{d_i}{D_i}\right)^2}, & \text{if } (b) - \text{neighbourhood defined as a sphere} \end{cases}$$

 D_s – spatial distance threshold; D_0, D_1, \dots, D_N - distance thresholds for other attributes $d_s, d_0, d_1, \dots, d_N$ – distances; d_s – distance in space

 $\begin{array}{l} \underline{\text{Distance in time }}(\mathsf{t}_1, \mathsf{t}_2 \text{ are intervals}):\\ d_t(t_1, t_2) = \begin{cases} t_2^{start} - t_1^{end} & if t_1^{end} < t_2^{start} \\ t_1^{start} - t_2^{end} & if t_1^{start} > t_2^{end} \\ 0 & otherwise \end{cases} \begin{array}{l} \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ d(v_1, v_2, \mathsf{V}) = \begin{cases} |v_1 - v_2|, & |v_1 - v_2| < \mathsf{V}/2 \\ |v_1 - v_2|, & otherwise \end{cases} \\ d(v_1, v_2, \mathsf{V}) = \{ v_1 - v_2 |, & otherwise \end{cases} \\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ d(v_1, v_2, \mathsf{V}) = \{ v_1 - v_2 |, & otherwise \end{cases} \\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ d(v_1, v_2, \mathsf{V}) = \{ v_1 - v_2 |, & otherwise \end{cases} \\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle length}):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle attribute }):\\ \underline{\text{Distance for a cyclic attribute }}(\mathsf{V} \text{ is the cycle attribute }):\\ \underline{\text{Distance for a cycle attribute }}(\mathsf{V} \text{ is the cycle attribute }):\\ \underline{\text{Distance f$




The STD-clusters, noise hidden







Step 3: unite STD-clusters in SD-clusters

Cluster the events from the STD-clusters by the spatial positions and directions



The result of the density-based clustering with the spatial distance threshold of 100 m and direction distance threshold of 20°





Events that occurred in same or close places but in different times were formerly in different clusters, but now they are in the same clusters.

One SD-cluster includes one or several STD-clusters.



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Step 4: outline the places of interest

Build spatial buffers around the SD-clusters of events



Rozzano

The places are painted according to the prevailing movement directions of the respective events.



Long area of congested movements directed to the west

Step 5: aggregate data by the places

and by suitable time intervals, e.g., hourly



Place-referenced time series of the counts of slow movement events

The temporal diagrams show the variation of the attribute value (vertical dimension) over time (horizontal dimension).



erra W (15) ✓ E (9) ✓ NW (7) ▼ N (6) SW (6) ✓ S (5) SE (4) NE (2)

Map fragment (northwest) enlarged

Congested traffic in the afternoon in the direction out of the city (northwest)

Congested traffic in the morning in the direction to the south





Where to read more

IEEE VAST 2011 paper (best paper award)

G.Andrienko, N.Andrienko, C.Hurter, S.Rinzivillo, S.Wrobel From Movement Tracks through Events to Places: Extracting and Characterizing Significant Places from Mobility Data *IEEE Visual Analytics Science and Technology (VAST 2011)*, Proceedings, IEEE Computer Society Press, 183-192

Extended version, covering also scalable clustering of events

G.Andrienko, N.Andrienko, C.Hurter, S.Rinzivillo, S.Wrobel Scalable Analysis of Movement Data for Extracting and Exploring Significant Places *IEEE Transactions on Visualization and Computer Graphics*, 2013, 19(7), 1078-1094



Perspective 3: Movement data in the form of spatial situations







Spatio-temporal aggregation of trajectories







Division of the territory

Characteristic points from the trajectories Spatial clusters of characteristic points

Cluster centres \rightarrow seeds for Voronoi tessellation



Details:

Natalia Andrienko, Gennady Andrienko

Spatial Generalization and Aggregation of Massive Movement Data

IEEE Transactions on Visualization and Computer Graphics (TVCG), 2011, v.17 (2), pp.205-219

http://doi.ieeecomputersociety.org/10.1109/TVCG.2010.44

Spatial situations: presence



Circle area is proportional to value:



Situation is described by tuples like <Place_id, time, attribute(s)>



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Spatial situations: flows



N moves by time intervals

0.00

^{91.00'} Situation is described by tuples like <Link_id, time, attribute(s)>



Clustering of spatial (flow) situations by similarity



Comparison of clusters of spatial situations



Where to read more

N.Andrienko, G.Andrienko, H.Stange, T.Liebig, D.Hecker Visual Analytics for Understanding Spatial Situations from Episodic Movement Data *Künstliche Intelligenz*, 2012, v.**26** (3), pp.241-251 http://dx.doi.org/10.1007/s13218-012-0177-4



Perspective 4: Movement data in the form of local time series





An alternative view of spatial time series: a set of local time series







An alternative view of spatial time series : a set of local time series



We wish to represent the essential characteristics of the ST-variation explicitly by a formal model or a set of models.



Methods for spatio-temporal modelling (e.g. STARIMA)

- Account for spatial and temporal dependencies
- Require prior specification of multiple weight matrices expressing impacts among locations for different temporal lags
 - may be difficult (the impacts are not easy to quantify)
- Build a single global model of the entire spatio-temporal variation
 - It does not necessarily perform better than a set of local temporal models
- Assume spatial smoothness of the modelled phenomenon, i.e., closer places are more similar than more distant ones
 - May be not very suitable for spatially abrupt phenomena





Existing techniques for time series modelling

- + Widely available in numerous statistical packages and libraries \rightarrow can be applied to spatially referenced time series
- The modelling methods are designed to deal with singular time series \rightarrow hard to use for a large number of time series
- Separate consideration of each time series ignores the phenomenon of spatial dependence (relatedness and similarities among spatial locations or objects)
- Separate consideration of each time series does not allow data abstraction and generalisation over space



Combination of spatial and temporal modelling

Approach 1:

- 1. Model the temporal variation independently for each location
- 2. Model the spatial variation of the parameters of the temporal models, e.g., as a random field
- Assumes that the character of the temporal variation is the same everywhere and only the parameters differ
- Approach 2:
 - Model the spatial variation independently for each time step, e.g., as a random field
 - Model the temporal variation of the parameters of the spatial models at each location
- Both approaches assume spatial smoothness of the phenomenon



Our approach

Details: Natalia Andrienko, Gennady Andrienko

A Visual Analytics Framework for Spatio-temporal Analysis and Modelling



Step 1: Clustering of local TS

- Here: k-means (Weka) but may be another partition-based method
- Tried different k from 5 to 15
- Immediate visual response facilitates choosing the most suitable k









Step 1: Re-grouping by progressive clustering





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N moves by hours
Check the presence of ordic variation of the data:
V Cycle: daily Sten: 1 hour Nofstens in cycle: 24 Cycle start in data: sten 0 A
Cycle: weakly Step: 1 hour Nofsteps in cycle: 168 Cycle start in data: step 24
Current class: 4 previous next Update classes Take other classes R
Perform modelling based on the C percentile 50 C mean V excluding 5 % of the V bighest V lowest values
Modelling method: triple exponential smoothing (Holt-winters) - D Kun modelling Show residuals Store model Restore model
Temporal cycles: Image: Single cycle; length = 24 steps Cycle start: step 24 C two cycles; inner cycle length = 24 steps; outer cycle consists of 7 inner cycles 0 additional time series E
alpha (overall smoothing) = 0.816406 beta (trend smoothing) = 0.0 gamma (seasonal smoothing) = 0.0
Store model set
Modelling Time extent (model) Time extent (view) Display Selection

- A) Check automatically detected time cycles in the data.
- B) Select the current class (cluster) for the analysis and modelling.
- C) Build the representative TS.
- D) Select the modelling method.
- E) View and modify model parameters (this section changes depending on the selected modelling method).











Step 3: Model evaluation (analysis of residuals)

- The goal is not to minimise the residuals
 - The model should not reproduce all fluctuations and outliers present in the data
 - This should be an abstraction capturing the characteristic features of the temporal variation
 - High values of the residuals do not mean low model quality
- The goal is to have the residuals randomly distributed in space and time (no detectable patterns)
 - This means that the model correctly captures the characteristic, nonrandom features of the temporal variation



Analysis of residuals (example)



- No systematic bias: approximately equal numbers of positive and negative errors in each time step
- No periodic increases and decreases at the level of the whole group
- However, we are not sure about individual objects



More detailed analysis by subgroups





It may be reasonable to consider this subgroup separately -> back to re-grouping

Use of a model for prediction

- We obtain a common model for a group (cluster) of time series
 - Predicts the same values for all objects/places of the group
 - The statistical properties of the distribution of the predicted values in each place differ from the distribution of the original values
- Adjustment of the prediction for individual objects/places:
 - Compute and store the basic statistics (quartiles) of the original values for each object/place i: Q1_i, M_i, Q3_i
 - Compute the statistics of the model-predicted values for the same time steps as the original values: Q1, M, Q3 (common for the cluster)
 - Shift (level adjustment): S = M_i M
 - Scale factors (amplitude adjustment): $F_{low} = \frac{M_i QI_i}{M QI}$ $F_{high} = \frac{Q3_i M_i}{Q3 M_i}$
 - Let v^t be the model-predicted value for an arbitrary time step t and v^t_i the individually adjusted value for the place/object i $V_{t_i} = \int M + F_{low} \cdot (v^t - M) + S$, if v^t < M

$$M + F_{high} \cdot (v^t - M) + S$$
, otherwise

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Use of a model for prediction: example

Common prediction for a cluster:



Set of individually adjusted predictions for this cluster:



Prediction based on the models







Comparison of actual values with predicted (e.g., in monitoring)

Absolute differences



-10.00

10.00

28.00

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-9.091

-3.000

3.000

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ONDON



Analysis and modelling of relationships between two time-variant attributes



Data transformation and clustering

- Dependency of attribute A(t) on attribute B(t):
 - Divide the value range of B into intervals
 - For each interval, collect all values of A that cooccur with the values of B from this interval
 - Compute statistics of the values of A: minimum, maximum, median, mean, percentiles ...
 - For each of these, there is a series $B \rightarrow A$, or A(B)





Dependencies of maximal flow magnitude on mean speed

Dependency modelling: flow \rightarrow maximal mean speed





Dependency modelling: mean speed \rightarrow maximal flow





Graphical representation of the models built





Use of the models: simulation of extraordinary traffic from given places		Gallaratese Trenno Lamaugnano 224
Set prediction models The simulation requires the following prediction models: 1. (Place_1, Place_2, Time) -> N of cars A set of time series models predicting the regular number of moves (flow) from one place to another by time intervals. Variation of N moves by hours *50: daily and weekly Select from available models 2. (Place_1, Place_2, N of cars) -> Possible speed 2) A set of dependency models predicting the maximal average speed of moving from one place to another depending on the place link load, i.e., number of cars that try to move. Variation of Max of Average speed (km/h) depending on N moves Select from available models 3. (Place_1, Place_2, Possible speed) -> N of cars A set of dependency models predicting the maximal number of cars (flow) that will be able to move from one place to another within a given time interval depending on the maximal average speed with which the cars can move. Variation of Max of N moves*50 depending on Average speed (km/h) Select from available models Scale factor for the model-predicted values: 1.0	Select the attribute defining the transition times. Start ID End ID N of moves Length Average move duration (minutes); total Average path length; km Average path length; km Average path length ratio to link length N trajectories; total *50 V Use the weights of the links defined by the attribute: Length Average path length; km Average path l	Image: Contract of the selected place(s) of origin: In place 171: 3000 In place 134:

Localize the places on map

The given number of objects will be distributed among the 3 selected places of origin.

Continue

Stop the process



ris, Descartes, CommonGIS, V-Analytics 1995-2010: Milan cars data aggregated by 1km areas

The bottlenecks can be revealed even before

_ _ _

Valayer2

Expected link load

Max: 3574

Min: 0 invert focus Dynamic map update Manipulate

▼ Data transformation

Simulated trajectories



Some traffic re-routed to the south:



The speeds on the northern motorway



Animation of simulation results



Presence and flows for selected time intervals



Multi-perspective analysis of movement





Bonus track: spatial decision support







Average hourly traffic flows and traffic jam events

Iris, Descartes, CommonGIS, V-Analytics 1995-2013: Traffic in Milan, 1 week





Traffic jam events summarized by areas and directions



Iris, Descartes, CommonGIS, V-Analytics 1995-2013: Traffic in Milan, 1 week



Traffic jam events summarized by areas and day times



Iris, Descartes, CommonGIS, V-Analytics 1995-2013: Traffic in Milan, 1 week



Traffic jam events summarized by links and day times





Multi-criteria choice support tool







Filtering by rank









Iris, Descartes, CommonGIS, V-Analytics 1995-2013: Traffic in Milan, 1 week





Iris, Descartes, CommonGIS, V-Analytics 1995-2013: Traffic in Milan, 1 week





Iris, Descartes, CommonGIS, V-Analytics 1995-2013: Traffic in Milan, 1 week





Iris, Descartes, CommonGIS, V-Analytics 1995-2013: Traffic in Milan, 1 week





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- Ch.2. Conceptual framework
- Ch.3. Transformations of movement data
- Ch.4. Visual analytics infrastructure
- Ch.5. Visual analytics focusing on movers
- Ch.6. Visual analytics focusing on spatial events
- Ch.7. Visual analytics focusing on space
- Ch.8. Visual analytics focusing on time
- Ch.9. Discussion and outlook

